# Designs for One-sided Neighbour Effects ${ }^{1}$ 

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#### Abstract

SUMMARY In agriculture and allied subjects, the treatment applied to one experimental plot may affect the response on neighbouring plots as well as response on the plot to which it is applied. The tall varieties may affect the other crops grown on the neighbouring plots by their shades. These effects are variously called neighbour effects or competition effects or interface effects. This paper is concerned with the study of one sided neighbour effect only. The merits and demerits of the designs are also discussed. Table and methods of applications for different designs are also presented.


Key words : One-sided neighbour effects, Border plot, Neighbourbalanced.

## 1. Introduction

In agriculture and allied subjects, the treatment applied to one experimental plot may affect the response on neighbouring plots as well as the response on the plot to which it is applied. In cereal crops or sunflowers, tall varieties may shade the plot on their North side ([13], [21]). In pesticide or fungicide experiments, part of the treatment may spread to the plot immediately downwind; so may spores from untreated plots [11]. These are both examples of one-sided effects. In plants with an important root system, such as potatoes, varieties $w^{\prime \cdot} \cdot \mathrm{h}$ germinate earlier will establish their roots and take nutrients from adjoining plots on both sides if the crop is grown in linear ridges [22], or on all sides if the crop is grown in a two-dimensional area with no gaps. Similar effects are reported on oil-seed rape [3], on field beans [4], in anti-feedants [20], in forestry [16] and in horticulture [8]. These effects are variously called neighbour effects or competition effects or interference effects.

This paper is concerned only with the first type of effect, the one-sided neighbour effect.

If the plots form a single long line, with plots numbered from 1 to $n$, assume that the neighbour effect is from plot $j$ to plot $j+1$. Denote by $T(j)$ the treatment on plot $j$. With a one-sided neighbour effect, the response on plot $j$

[^0]depends both on $T(j)$ and $T(j-1)$. Some suitable designs for this situation have been given by Finney and Outhwaite [10], Dyke and Shelley [9] and Lewis [17].

However, it is more common to arrange the plots in separated linear blocks. Assume that there are b blocks of size k, and v treatments. Now denote by $T(i, j)$ the treatment on plot $j$ of block $i$, and by $Y_{i j}$ the response on that plot.

## 2. Models and Effects

The simplest model for a one-sided neighbour effect is

$$
\begin{equation*}
E\left(Y_{i j}\right)=\beta_{i}+\tau_{T(i, j)}+\alpha_{T(i, j-1)} \tag{1}
\end{equation*}
$$

and

$$
\operatorname{Cov}(\mathbf{Y})=\sigma^{2} \mathbf{I}
$$

where $\beta_{1}, \ldots, \beta_{b}$ are (unknown) block effects, $\tau_{1}, \ldots, \tau_{v}$ are (unknown) direct effects of the treatments, $\alpha_{1}, \ldots, \alpha_{v}$ are (unknown) neighbour effects of the treatments, and $\sigma^{2}$ is the (unknown) variance per plot.

Some more complicated models for $E\left(Y_{i j}\right)$ have been proposed. One is that

$$
E\left(Y_{i j}\right)=\left\{\begin{array}{cc}
\beta_{i}+\tau_{T(i, j)}+\alpha_{T(i, j-1)} & \text { if } T(i, j) \neq T(i, j-1)  \tag{2}\\
\beta_{i}+\tau_{T(i, j)} & \text { if } T(i, j)=T(i, j-1)
\end{array}\right.
$$

This is tantamount to saying that each treatment has no neighbour effect on itself. For example, it may be argued that tall sunflowers shade shorter varieties but not other sunflowers of the same height. However, photosynthesis occurs in all the leaves of a plant, so a plant growing next to another plant of the same variety can clearly make less use of the sun than a plant with no shading.

What the experimenter usually seeks to find is the overall effect of a treatment when it is grown throughout a field ([5], [12]). If treatment x is applied to every plot in block i then, under model (1)

$$
E\left(Y_{i j}\right)=\beta_{i}+\phi_{x}
$$

where $\phi_{x}=\tau_{x}+\alpha_{x}$. We call $\phi_{x}$ the total effect of treatment $x$. I think that those who have proposed model (2) have confused $\tau_{x}$ with $\phi_{x}$.

A further model ([15], [21]) which may confuse the direct and total effects is

$$
E\left(Y_{i j}\right)=\left\{\begin{array}{cc}
\beta_{i}+\tau_{T(i, j)}+\alpha_{T(i, j-1)} & \text { if } T(i, j) \neq T(i, j-1)  \tag{3}\\
\beta_{i}+\tau_{T(i, j)}+\gamma_{T(i, j)} & \text { if } T(i, j)=T(i, j-1)
\end{array}\right.
$$

In this case $\phi_{x}=\tau_{x}+\gamma_{x}$

More complicated still is the model which allows for full interaction between a treatment and its neighbour ([12], [22])

$$
\begin{equation*}
E\left(Y_{i j}\right)=\beta_{i}+\tau_{T(i, j)}+\alpha_{T(i, j-1)}+\delta_{T(i, j), T(i, j-1)} \tag{4}
\end{equation*}
$$

In this case $\phi_{\mathrm{x}}=\tau_{\mathrm{x}}+\alpha_{\mathrm{x}}+\delta_{\mathrm{xx}}$
There is a large literature on designs for the estimation of direct effects $\tau$. For example, Philippeau et al. [19] recommend that, if model (1) is appropriate, then it is efficient to use a neighbour-balanced design (to be defined in Section 3 ) and analyse for the simple model with no neighbour effects. Kunert and Stufken [15] assume model (3) and recommend designs in which the $\gamma$ parameters are not estimable.

However, the aim of the experiment is surely to estimate the total effects $\phi$. If model (2) or (3) or (4) holds, then the $\alpha$ parameters (and $\delta$ parameters, if any) are of no interest but the $\gamma$ parameters (if any) are important. In this situation the only sensible way to conduct the experiment is to apply treatments to large areas such as whole fields, with guard areas in between. This is likely to be much more expensive, have smaller true replication, and have larger variability than an experiment in smaller plots.

If model (1) holds then we can still conduct an experiment in small plots in linear blocks. There is a difficulty about plot 1 of each block, because there is apparently no neighbour effect to apply to it. However, we should really include a parameter $\alpha_{0}$ for the effect of 'no neighbour'. Rather than fit this extra parameter, an alternative that is often recommended is to have a border plot before plot 1 of each block i. A treatment $\mathrm{T}(\mathrm{i}, 0)$ is applied to this plot but its response is not measured. It is convenient if $\mathrm{T}(\mathrm{i}, 0)=\mathrm{T}(\mathrm{i}, \mathrm{k})$, because then each neighbour effect occurs the same number of times in block j as its corresponding direct effect. A bordered block design with this property is called circular.

There is now a design dilemma. To estimate $\tau_{\mathrm{x}}+\alpha_{\mathrm{x}}$ well, we need many adjacent pairs of plots that both have treatment $x$. On the other hand, to allow for block effects efficiently, we do not want any treatment to occur more than once in any block, if $\mathrm{k} \leq \mathrm{v}$. However, adjacent plots are always in the same block if blocks are well separated.

Bailey and Druilhet [4] sought to resolve this dilemma by finding circular block designs which are optimal for estimation of the total effects $\phi$. They showed that if no treatment is ever adjacent to itself then circular block designs which are binary (no treatment occurs more than once in a block), balanced (in the usual sense that every pair of distinct treatments is in the same number of blocks) and neighbour-balanced, are optimal for the estimation of total effects. Azais et al. [2] gave a table of such designs for $\mathrm{b}=\mathrm{v}, \mathrm{k}=\mathrm{v}-1$ and $\mathrm{b}=\mathrm{v}-1$, $\mathrm{k}=\mathrm{v}$, with instruction for their use.

Bailey and Druilhet also showed that if $b$ if large then designs with selfneighbours are better than those without, if $k \geq 5$. They describe a class of optimal designs which can certainly be realised if $b=v$ !, which is usually too large for practical use. The remainder of this paper gives optimal designs for the smallest possible value of $b$, for given small values of $k$ and $v$.

## 3. Properties of the Designs

Each design is balanced in the sense that there is an integer $\mu$ such that every pair of distinct treatments has concurrence $\mu$. Here the concurrence of treatments $x$ and $y$ means the number of pairs of plots in the same block with one receiving treatment $x$ and the other receiving treatment $y$. Each design is also neighbour-balanced in the sense that there is an integer $\lambda$ such that every treatment is followed by each other treatment $\lambda$ times.

Bailey and Druilhet [4] give the optimal number $s$ of treatments to put in each block, for each block size $k$ with $3 \leq k \leq 16$. Part of this information is reproduced in Table 1 . When $k=4$ there are three values of $s$, all optimal. Of the $s$ treatments in any block, $n_{1}$ occur $m$ times and $n_{2}$ occur $m+1$ times, where $m$ is the integer part of $k / s, n_{2}=k-s m$ and $n_{1}=s-n_{2}$. Each block contributes $\theta / 2$ to the sum of the concurrences, where

$$
\begin{aligned}
\theta & =n_{1}\left(n_{1}-1\right) m^{2}+n_{2}\left(n_{2}-1\right)(m+1)^{2}+2 n_{1} n_{2} m(m+1) \\
& =\operatorname{sm}(m+1)+k(k-2 m-1)
\end{aligned}
$$

Hence

$$
\begin{equation*}
\mathrm{b} \theta=\mathrm{v}(\mathrm{v}-1) \mu \tag{5}
\end{equation*}
$$

Bailey and Druilhet [4] show that all occurrences of any one treatment in any one block must be in a single sequence of adjacent plots (possibly including both the last plot and the first plot), so each block contributes $s$ to the sum of neighbour adjacencies. Hence

$$
\begin{equation*}
b s=v(v-1) \lambda \tag{6}
\end{equation*}
$$

Table 1. When the blocks have size $k$, then $s$ treatments should appear in each block, with $n_{1}$ appearing $m$ times and $n_{2}$ appearing $m+1$ times, so each block contributes $\theta$ to the sum of the concurrences

| k | 3 | 4 | 4 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| s | 3 | 2 | 3 | 4 | 3 | 3 | 4 | 4 | 4 |
| m | 1 | 2 | 1 | 1 | 1 | 2 | 1 | 2 | 2 |
| $\mathrm{n}_{1}$ | 3 | 2 | 2 | 4 | 1 | 3 | 1 | 4 | 3 |
| $\mathrm{n}_{2}$ | 0 | 0 | 1 | 0 | 2 | 0 | 3 | 0 | 1 |
| $\theta$ | 6 | 8 | 10 | 12 | 16 | 24 | 36 | 48 | 60 |

Note that if $\theta$ and $s$ are coprime then $b$ must be a multiple of $v(v-1)$.

## 4. The Tables, and How to Use Them

Tables 3-6, supplemented by the text in Section 5, give the smallest designs with the properties in Section 3, for the range $3 \leq k \leq 9$ and $\mathrm{s} \leq \mathrm{v} \leq 10$. Apart from the exceptions mentioned in Section 5, each given design has the parameters which are the smallest solutions to Equations (5) and (6).

To use these, first choose one of the designs for the appropriate values of $v$ and $k$. If $k=4$ there may be a choice of design. In the tables, the blocks are shown as columns, to save space. Randomly allocate the columns of the chosen design to the actual blocks. In each block independently, randomly choose a number $l$ between 1 and $k$ inclusive, and move the treatment on plot $i$ to plot $i+l$ modulo $k$. Finally, in each block, put the treatment on plot $k$ onto the border plot before plot 1 .

For example, if $v=k=5$ then start with the design in Table 5(a), which has 20 blocks. Randomization can produce the layout in Table 2, where the blocks are shown as rows, with the border plot at the left-hand end.

Table 2. One layout obtained by randomizing the design in Table 5(a)

| 5 | 1 | 1 | 2 | 2 | 5 | 3 | 1 | 1 | 5 | 3 | 3 | 5 | 2 | 2 | 3 | 5 | 5 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 2 | 4 | 4 | 5 | 2 | 5 | 4 | 4 | 3 | 3 | 5 | 4 | 2 | 2 | 5 | 5 | 4 | 4 |
| 3 | 1 | 2 | 2 | 3 | 3 | 1 | 4 | 4 | 2 | 2 | 1 | 1 | 1 | 4 | 5 | 5 | 1 | 1 |
| 5 | 5 | 1 | 3 | 3 | 5 | 5 | 5 | 4 | 4 | 1 | 5 | 3 | 4 | 1 | 1 | 3 |  | 3 |
| 2 | 3 | 3 | 4 | 4 | 2 | 5 | 5 | 3 | 3 | 2 | 5 | 2 | 2 | 1 | 1 | 3 | 2 | 2 |
| 1 | 1 | 2 | 4 | 4 | 1 | 1 | 5 | 5 | 2 | 1 | 1 | 3 | 3 | 2 | 2 | 4 | 3 | 3 |
| 4 | 4 | 5 | 5 | 3 | 4 | 3 | 1 | 1 | 4 | 4 | 3 |  |  |  |  |  |  |  |

## 5. Tables of Designs

### 5.1 Block Size Three

When $\mathrm{k}=3$ then $\mathrm{s}=3$ and the designs are just Mendelsohn triple systems [18]. As Colburn and Rosa [7] show, there is a design corresponding to the smallest integer solutions of Equations (5) and (6) except when $v=6$. These are given in Table 3. The second smallest solution for $v=6$ corresponds to the design in Table 3(d).

Table 3. Designs for blocks of size $3(k=3, s=3, \theta=6)$
11
23
32
(a) $v=3, b=2, \mu=2, \lambda=1$

3412
1234
2143
(b) $v=4, b=4, \mu=2, \lambda=1$
$\begin{array}{lllllllllllllllllllll}1 & 3 & 1 & 4 & 1 & 5 & 1 & 4 & 1 & 5 & 1 & 5 & 2 & 4 & 2 & 5 & 2 & 5 & 3 & 5\end{array}$
$\begin{array}{lllllllllllllllllll}2 & 2 & 2 & 2 & 2 & 2 & 3 & 3 & 3 & 3 & 4 & 4 & 3 & 3 & 3 & 3 & 4 & 4 & 4\end{array} 4$
$\begin{array}{lllllllllllllllllll}3 & 1 & 4 & 1 & 5 & 1 & 4 & 1 & 5 & 1 & 5 & 1 & 4 & 2 & 5 & 2 & 5 & 2 & 5\end{array}$
(c) $v=5, b=20, \mu=6, \lambda=3$

12345123456666651234
23451345122345134512
66666512341234512345
(d) $v=6, b=20, \mu=4, \lambda=2$

12345674567123
23456712345671
45671231234567
(e) $v=7, b=14, \mu=2, \lambda=1$

1234567888888888888888888888
4567123712345671234567123456
2345671123456723456714567123
1234567123456712345671234567
3456712234567167123455671234
5671234345671223456712345671
(f) $v=8, b=56, \mu=6, \lambda=3$

134679172839192738182937
225588445566556644664455
316497718293917283819273
(g) $v=9, b=24, \mu=2, \lambda=1$

147000000000172839192738182937
258564231897445566556644664455
369456123789718293917283819273
(h) $v=10, b=30, \mu=2, \lambda=1$

### 5.2 Block Size Four

When $k=4$ then $s$ may be 2 or 3 or 4 . If $s=2$ then each block has the cyclic pattern ( $x, x, y, y$ ). Using one such block for each unordered pair $\{x, y\}$ of treatments gives a design with $b=v(v-1) / 2$. The designs in parts (a), (c), (f), (h), (j) and (1) of Table 4 have this form. If $s=3$ then Equations (5) and (6) give $10 \mathrm{~b}=\mathrm{v}(\mathrm{v}-1) \mu$ and $3 \mathrm{~b}=\mathrm{v}(\mathrm{v}-1) \lambda$, whose smallest integer solution has $b=v(v-1)$, so these designs are no improvement on those with $s=2$ and therefore none are shown in Table 4.

When $s=4$ the designs are known as oriented balanced incomplete-block designs or perfect Mendelsohn designs [18], and are related to directed Whist tournaments [1]. Now Equations (5) and (6) give $\mu=3 \lambda$ and $4 b=v(v-1) \lambda$. Table 4 includes designs for the smallest integer solutions to these equations except for $v=4$ (when trial and error quickly shows that there is no solution with $b=3$ ), and $v=8$ (where [6] shows that there is no solution with $b=14$ ).

Table 4. Designs for blocks of size four $(k=4)$
112
112
233
233
(a) $v=3, s=2, b=3, \theta=8, \mu=4, \lambda=1$

111222
234144
342431
423313
(b) $v=4, s=4, b=6, \theta=12, \mu=6, \lambda=2$

111223
111223
234344
234344
(c) $v=4, s=2, b=6, \theta=8, \mu=4, \lambda=1$

12345
23451
45123
34512
(d) $v=5, s=4, b=5, \theta=12, \mu=3, \lambda=1$

```
    666666666622223
    112352344544515
    231145435253154
    344511252331431
(e) v=6,s=4,b=15,0=12,\mu=6,\lambda=2
    111112222333445
    111112222333445
    234563456456566
    234563456456566
(f) v=6,s=2,b=15,0=8,\mu=4,\lambda=1
    712345671234567123456
    123456712345672345671
    345671245671236712345
    234567134567124567123
(g) v = 7, s=4,b=21, 0=12, \mu =6,\lambda =2
    111111222223333444556
    111111222223333444556
    234567345674567567677
    234567345674567567677
(h)}v=7,s=2,b=21,0=8,\mu=4,\lambda=
7123456888888845671232345671
1234567123456723456716712345
2345671671234512345671234567
4567123234567171234568888888
(i) \(\mathrm{v}=8, \mathrm{~s}=4, \mathrm{~b}=28, \theta=12, \mu=6, \lambda=2\)
1111111222222333334444555667
1111111222222333334444555667
2345678345678456785678678788
2345678345678456785678678788
(j) \(v=8, s=2, b=28, \theta=8, \mu=4, \lambda=1\)
564231897231897564
645312978456123789
978645312312978645
897564231789456123
(k) \(v=9, s=4, b=18, \theta=12, \mu=3, \lambda=1\)
```

```
    111111111222222223333333444444
    111111111222222223333333444444
    234567890345678904567890567890
    234567890345678904567890567890
    555556666777889
    555556666777889
    678907890890900
    678907890890900
(l) v=10,s=2,b=45,0=8,\mu=4,\lambda=1
    123456789123456789123456789
    234567891345678912456789123
    678912345234567891912345678
    456789123789123456678912345
```

    000000000000000000
    123456789123456789
    234567891912345678
    456789123789123456
    (m) $\mathrm{v}=10, \mathrm{~s}=4, \mathrm{~b}=45, \theta=12, \mu=6, \lambda=2$
5.3 Block Size Five

When $k=5$ then $s=3$, so Equations (5) and (6) give $16 b=v(v-1) \mu$ and $3 b=v(v-1) \lambda$, so $b$ must be a multiple of $v(v-1)$. If $v=3,4,7,9$ or 10 then Table 3 gives a design with $s=k=3$ and $b=v(v-1) / 3$. Replace each block of the form ( $x, y, z$ ) by the three blocks ( $x, y, y, z, z$ ), $(x, x, y, z, z)$ and ( $x, x, y, y$, $z)$. Designs for $v=5,6$ and 8 with $b=v(v-1)$ are given in Table 5 .
Table 5. Designs for blocks of size five $(k=4, s=3, \theta=16)$ : see text for other numbers of treatments

```
12345234513451245123
23451451231234534512
23451451231234534512
34512123454512323451
34512123454512323451
```

(a) $v=5, b=20, \mu=16, \lambda=3$

666661234523451512344512345123
234513451251234666663451251234
234513451251234666663451251234
123454512366666234515123434512
123454512366666234515123434512
(b) $v=6, b=30, \mu=16, \lambda=3$

| 2 | 3 | 4 | 5 | 6 | 7 | 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 8 | 8 | 8 | 8 | 8 | 8 | 7 | 1 | 2 | 3 | 4 | 5 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | 6

3456712234567167123455671234
5671234345671223456712345671
5671234345671223456712345671
1234567123456712345671234567
1234567123456712345671234567
(c) $v=8, b=56, \mu=16, \lambda=3$

### 5.4 Block Size Six

When $k=6$ then $s=3$ and every block has the form ( $x, x, y, y, z, z$ ). Use the design from Table 3 for the appropriate value of $v$, and double the occurrences of each entry. For example, if $v=7$ then the first block is ( $1,1,2,2$, 4, 4). Note that, after randomization, there are six possibilities for this block, including

| 2 | 4 | 4 | 1 | 1 | 2 | 2 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | and | 4 | 4 | 1 | 1 | 2 | 2 | 4 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

### 5.5 Block Size Seven

When $k=7$ then $s=4$, so Equations (5) and (6) give $\mu=9 \lambda$ and $4 \mathrm{~b}=\mathrm{v}(\mathrm{v}-1) \lambda$. Also, every within-block contribution to concurrence is either 4 or 2 , so $\mu$ is even and hence $\lambda$ is even. Each block has a single unrepeated treatment, so, to maintain symmetry, $b$ must be a multiple of $v$. Table 6 shows the smallest design for $v=4,6,7,8$ and 9 .

When $v=5$, use the design in Table 4 with $s=4$ and replace each block of the form ( $w, x, y, z$ ) by the four blocks ( $w, x, x, y, y, z, z$ ) $(w, w, x, y, y, z, z)$, ( $w, w, x, x, y, z, z$ ) and ( $w, w, x, x, y, y, z$ ).

When $v=10$ the smallest solution to the equations has $b=90$. A design with 90 blocks of 7 plots each is probably too large for practical purposes, so no design is tabulated.

### 5.6 Block Size Eight

When $k=8$ then $s=4$ and every block has the form ( $w, w, x, x, y, y, z, z$ ). Use the design from Table 4 for the appropriate value of $v$ with $s=4$, and double the occurrence of each entry.

### 5.7 Block Size Nine

When $k=9$ then $s=4$ and again we find that $4 b=v(v-1) \lambda, \lambda$ is even and $v$ divides $b$. Use the designs for $k=7$ and replace each block of the form ( $w, x, x, y, y, z, z$ ) by the block ( $w, w, w, x, x, y, y, z, z$ ).

Table 6. Designs for blocks of size seven $(k=7, s=4, \theta=36)$ : see text for other numbers of treatments

```
123423311244
214331234412
214331234412
341212442331
432144123123
432144123123
```

(a) $v=4, b=12, \theta=36, \lambda=4$

> 644523632556153413161224263514
> 435236344345564635624152312323
> 435236344345564635624152312323
> 352665425214636154256415621241
> 352665425214636154256415621241
> 566452263451311341512641135132
> 566452263451311341512641135132
> (b) $v=6, b=30, \mu=36, \lambda=4$

712345612345677123456
123456745671232345671
123456745671232345671
345671234567126712345
345671234567126712345
234567171234564567123
234567171234564567123
(c) $v=7, b=21, \mu=18, \lambda=2$

7123456123456723456714567123
1234567234567112345672345671
1234567234567112345672345671
2345671456712371234561234567
2345671456712371234561234567
4567123712345645671237123456 4567123712345645671237123456

8888888123456767123452345671 1234567671234512345676712345
1234567671234512345676712345
6712345234567188888881234567
6712345234567188888881234567
2345671888888823456718888888 2345671888888823456718888888
(d) $v=8, b=56, \mu=36, \lambda=4$
123789456456123789123789456645312978
2318975641237894566453112978231897564
23189756412378945664531129782311897564
564231897231897564231897564978654312
564231897231897564231897564978654312
456123789564231897978645312123789456
456123789564231897978645312123789456
(e) $v=9, b=36, \mu=18, \lambda=2$

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